



1. Find the quotient

$$\frac{(6+2j)-(1+3j)}{(-1+j)-2}.$$

2. Let k be an integer. Show that

(a) $j^{4k} = 1$,

(b) $j^{4k+1} = j$,

(c) $j^{4k+2} = -1$,

(d) $j^{4k+3} = -j$.

3. Find

(a) j^7 ,

(b) j^{62} ,

(c) j^{-202} ,

(d) j^{-4321} .

4. Evaluate

$$3j^{11} + 6j^3 + \frac{8}{j^{20}} + j^{-1}.$$

5. Solve each of the following equations for z .

(a) $jz = 4 - zj$,

(b) $\frac{z}{1-z} = 1 - 5j$,

(c) $(2-j)z + 8z^2 = 0$,

(d) $z^2 + 16 = 0$.

6. Let $z = 3 - 2j$. Plot the following points in the complex plane

(a) z ,

(b) $-z$,

(c) $\bar{z}$,

(d) $-\bar{z}$,

(e) $\frac{1}{z}$.

7. Find $\arg(1 + \sqrt{3}j)$ and write $1 + \sqrt{3}j$ in polar form.

8. Write the quotient

$$\frac{(1+j)}{(\sqrt{3}-j)}$$

in polar form.

9. Compute by using Euler's equation

(a) $(1+j)/(\sqrt{3}-j)$,

(b) $(1+j)^{24}$.

Hint: Euler's equation

$$e^{jy} = \cos y + j \sin y$$

10. Prove De Moivre's formula

$$(\cos \theta + j \sin \theta)^n = \cos n\theta + j \sin n\theta, \quad n = 1, 2, 3, \dots$$

$$\text{for } (1+j)^{24}.$$

11. Write $e^{-j\pi/4}$ in the form of $a + bj$.

12. Write $(1+j)^6$ in the polar form $re^{j\theta}$.

13. Solve

$$z^2 - (3-2j)z + 1 - 3j = 0.$$

14. Prove that the function

$$f(z) = e^z = e^x \cos y + je^x \sin y$$

is entire, and find its derivative.

15. Construct an analytic function whose real part is

$$u(x, y) = x^3 - 3xy^2 + y.$$